

Write your name here

Surname

Other names

**Pearson Edexcel**  
**Level 3 GCE**

Centre Number

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Candidate Number

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# Mathematics

**Advanced**

**Paper 2: Pure Mathematics 2**

Wednesday 13 June 2018 – Morning

**Time: 2 hours**

Paper Reference

**9MA0/02**

**You must have:**

Mathematical Formulae and Statistical Tables, calculator

Total Marks

**Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

## Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Answers should be given to three significant figures unless otherwise stated.

## Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 14 questions in this question paper. The total mark for this paper is 100.
- The marks for each question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

## Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end

Turn over ►

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Answer ALL questions. Write your answers in the spaces provided.

1.

$$g(x) = \frac{2x + 5}{x - 3} \quad x \geq 5$$

- (a) Find  $gg(5)$ . (2)
- (b) State the range of  $g$ . (1)
- (c) Find  $g^{-1}(x)$ , stating its domain. (3)

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2. Relative to a fixed origin  $O$ ,

the point  $A$  has position vector  $(2\mathbf{i} + 3\mathbf{j} - 4\mathbf{k})$ ,

the point  $B$  has position vector  $(4\mathbf{i} - 2\mathbf{j} + 3\mathbf{k})$ ,

and the point  $C$  has position vector  $(a\mathbf{i} + 5\mathbf{j} - 2\mathbf{k})$ , where  $a$  is a constant and  $a < 0$

$D$  is the point such that  $\overrightarrow{AB} = \overrightarrow{BD}$ .

(a) Find the position vector of  $D$ .

(2)

Given  $|\overrightarrow{AC}| = 4$

(b) find the value of  $a$ .

(3)

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3. (a) "If  $m$  and  $n$  are irrational numbers, where  $m \neq n$ , then  $mn$  is also irrational."

**Disprove** this statement by means of a counter example.

(2)

- (b) (i) Sketch the graph of  $y = |x| + 3$

(ii) Explain why  $|x| + 3 \geq |x + 3|$  for all real values of  $x$ .

(3)

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4. (i) Show that  $\sum_{r=1}^{16} (3 + 5r + 2^r) = 131\,798$  (4)

(ii) A sequence  $u_1, u_2, u_3, \dots$  is defined by

$$u_{n+1} = \frac{1}{u_n}, \quad u_1 = \frac{2}{3}$$

Find the exact value of  $\sum_{r=1}^{100} u_r$  (3)

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6.

$$f(x) = -3x^3 + 8x^2 - 9x + 10, \quad x \in \mathbb{R}$$

(a) (i) Calculate  $f(2)$ (ii) Write  $f(x)$  as a product of two algebraic factors.

(3)

Using the answer to (a)(ii),

(b) prove that there are exactly two real solutions to the equation

$$-3y^6 + 8y^4 - 9y^2 + 10 = 0$$

(2)

(c) deduce the number of real solutions, for  $7\pi \leq \theta < 10\pi$ , to the equation

$$3 \tan^3 \theta - 8 \tan^2 \theta + 9 \tan \theta - 10 = 0$$

(1)

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9. Given that  $\theta$  is measured in radians, prove, from first principles, that

$$\frac{d}{d\theta}(\cos \theta) = -\sin \theta$$

You may assume the formula for  $\cos(A \pm B)$  and that as  $h \rightarrow 0$ ,  $\frac{\sin h}{h} \rightarrow 1$  and  $\frac{\cos h - 1}{h} \rightarrow 0$   
(5)

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10. A spherical mint of radius 5 mm is placed in the mouth and sucked.  
Four minutes later, the radius of the mint is 3 mm.

In a simple model, the rate of decrease of the radius of the mint is inversely proportional to the square of the radius.

Using this model and all the information given,

- (a) find an equation linking the radius of the mint and the time.  
(You should define the variables that you use.) (5)
- (b) Hence find the total time taken for the mint to completely dissolve. Give your answer in minutes and seconds to the nearest second. (2)
- (c) Suggest a limitation of the model. (1)

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12. (a) Prove that

$$1 - \cos 2\theta \equiv \tan \theta \sin 2\theta, \quad \theta \neq \frac{(2n+1)\pi}{2}, \quad n \in \mathbb{Z} \quad (3)$$

(b) Hence solve, for  $-\frac{\pi}{2} < x < \frac{\pi}{2}$ , the equation

$$(\sec^2 x - 5)(1 - \cos 2x) = 3 \tan^2 x \sin 2x$$

Give any non-exact answer to 3 decimal places where appropriate.

(6)

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14. A scientist is studying a population of mice on an island.

The number of mice,  $N$ , in the population,  $t$  months after the start of the study, is modelled by the equation

$$N = \frac{900}{3 + 7e^{-0.25t}}, \quad t \in \mathbb{R}, \quad t \geq 0$$

(a) Find the number of mice in the population at the start of the study.

(1)

(b) Show that the rate of growth  $\frac{dN}{dt}$  is given by  $\frac{dN}{dt} = \frac{N(300 - N)}{1200}$

(4)

The rate of growth is a maximum after  $T$  months.

(c) Find, according to the model, the value of  $T$ .

(4)

According to the model, the maximum number of mice on the island is  $P$ .

(d) State the value of  $P$ .

(1)

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Question 14 continued

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Lined writing area for the answer to Question 14.



